

# **PHYSICAL PROPERTIES OF BIOMATERIALS LIKE SHAPE, SIZE, VOLUME AND SURFACE AREA**

Lecture 3 & 4

PFE-2.4.5

By:

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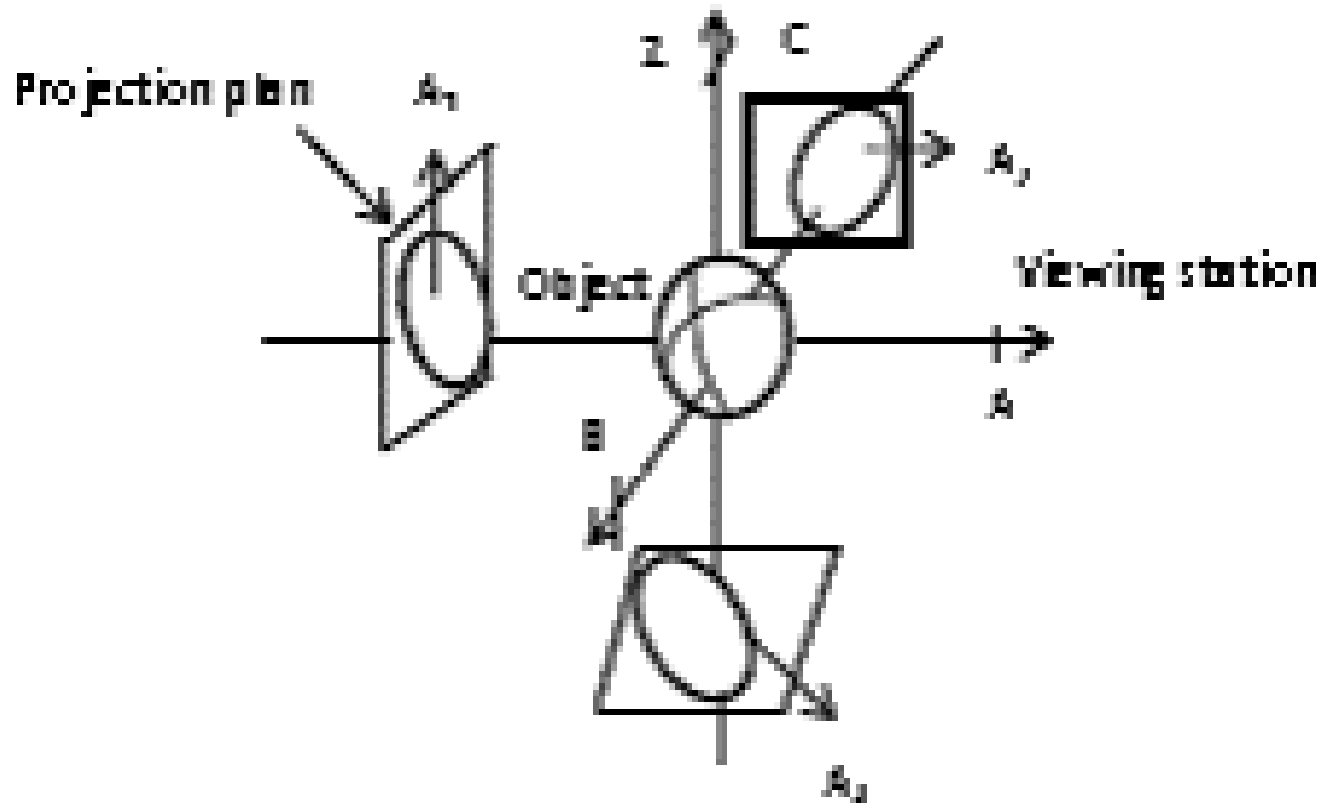
# SIZE

- Size is an important physical attribute of foods used in **screening** solids to separate foreign materials, **grading** of fruits and vegetables, and evaluating the **quality** of food materials.
- **Sorting of fresh market** - Pattern packing, higher packing density
- Modern or on-line fruit/ vegetables/ grain/spices density sorting.
- **Surface area** - Quantifying the microbial population
- internal quality (IQ) sensors
- **some primary and secondary processing machines**

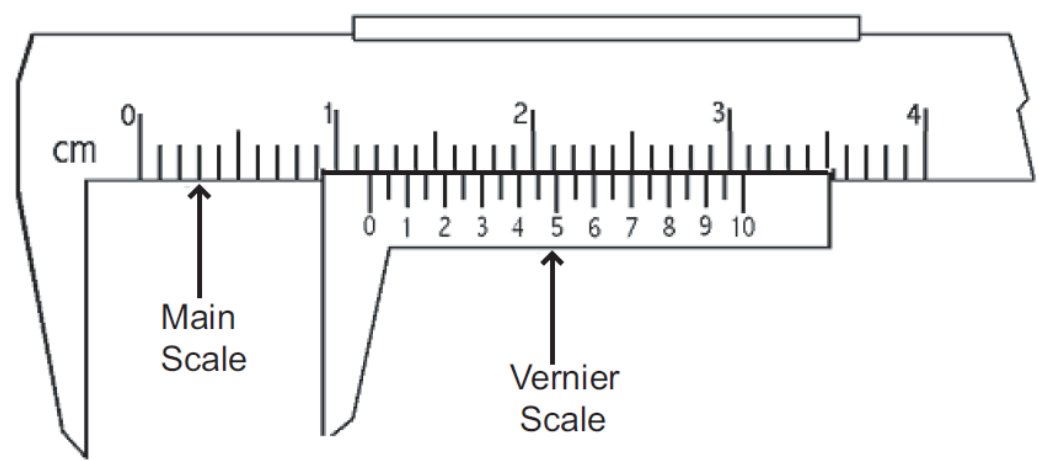
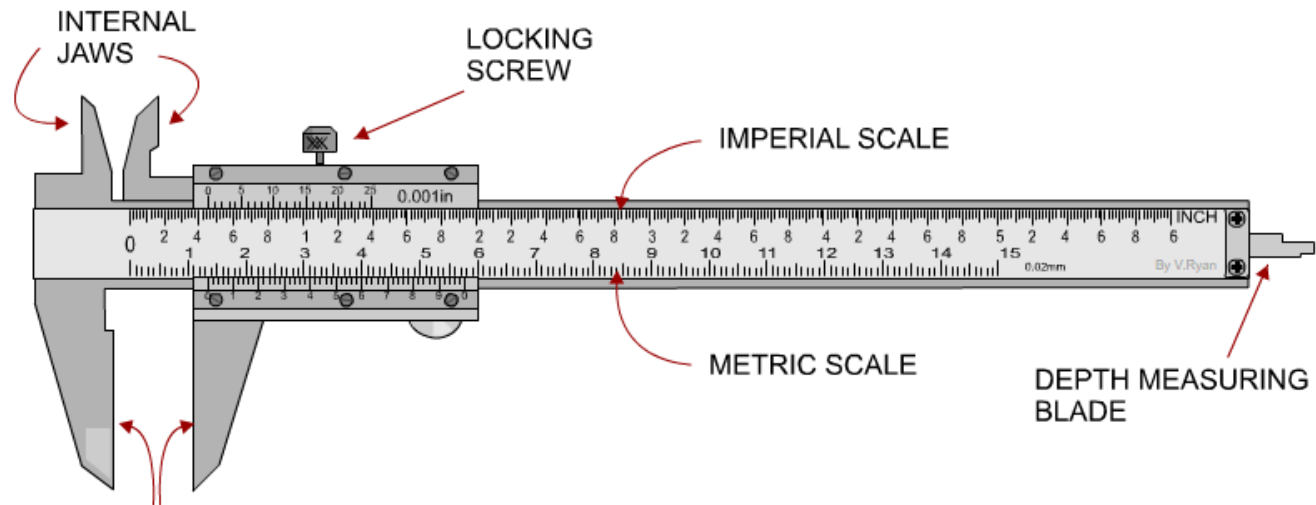
# Methods of measurement of size

- **Projected area method**
  - **Major diameter**, which is the longest dimension of the maximum projected area
  - **Intermediate diameter**, which is the minimum diameter of the maximum projected area or the maximum diameter of the minimum projected area.
  - **Minor diameter**, which is the shortest dimension of the minimum projected area.

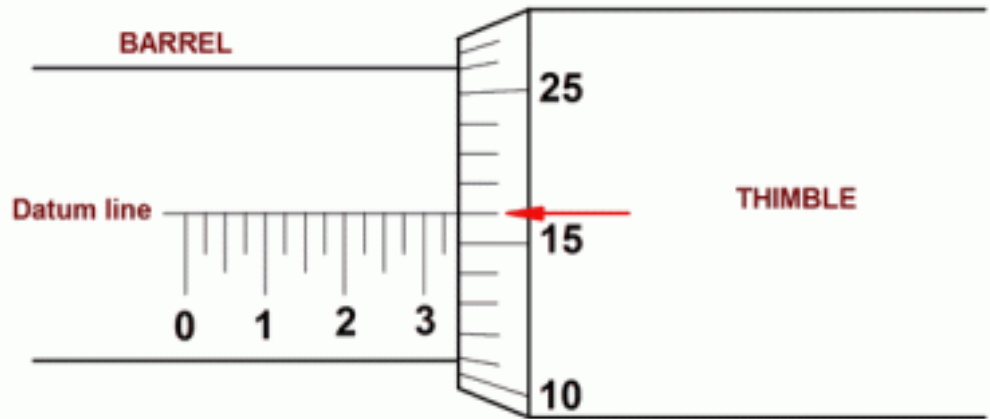
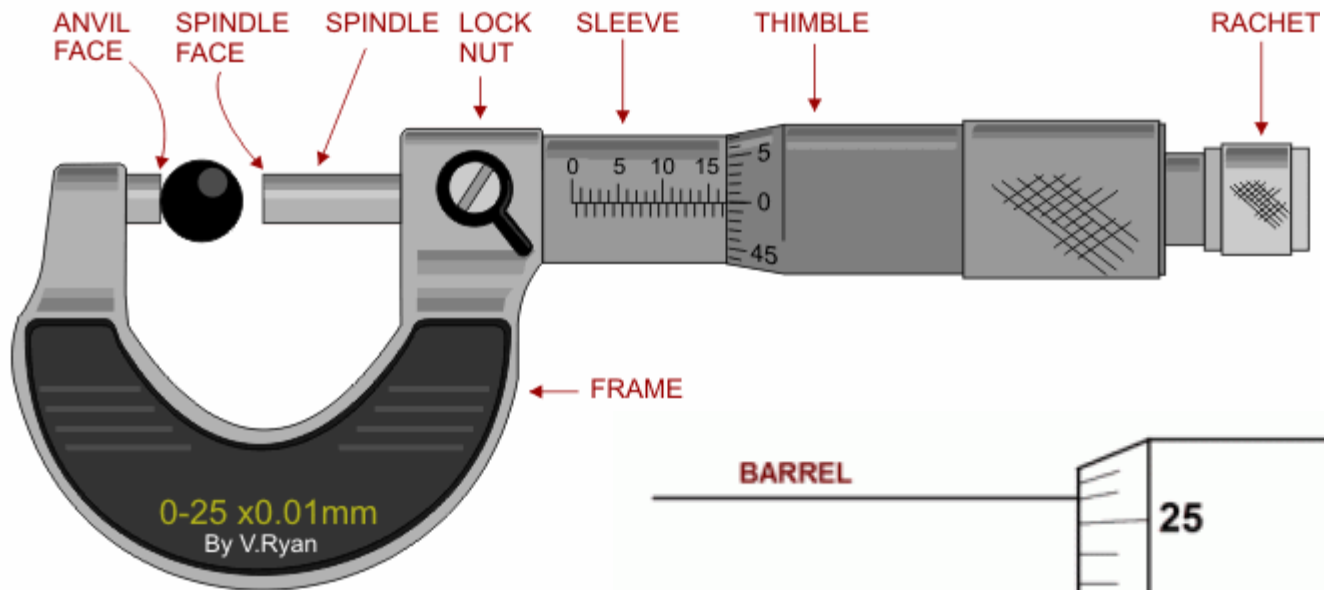
# Projected area method



# Vernier caliper



# Micrometer measurement



# Grain shape tester



- Place a small quantity of sample on the plate
- Operate the lever by left hand.
- Holding a pencil by right hand
- Measure the grain length or thickness by moving each grain to the groove.

# Electronic system

- Volume of the gap between the fruit and the outer casing of **embracing gauge equipment**.
- Systems that calculate fruit size by measuring the distance between a **radiation source** and the fruit
- Systems that rely on the **obstruction of light barriers**
- Two-dimensional (**2-D**) machine vision systems such as digital images received by **web cameras, CCD cameras**.
- **Three-dimensional (3-D)** machine vision systems such as multi spectral and hyper-spectral imaging system.
- **Computed tomography (CT)**- It is a technology that uses computer-processed x-rays to produce tomographic images (virtual 'slices') of specific areas of the scanned object, allowing the user to see what is inside it without cutting it open.)
- **Magnetic resonance imaging (MRI), X-ray, ultrasound** techniques as well as some other approaches not included in the other groups.



# SHAPE

- **Heat and mass transfer calculations,**
- **Screening solids to separate foreign materials**
- **Grading of fruits**
- **quality of food materials**

# Shape

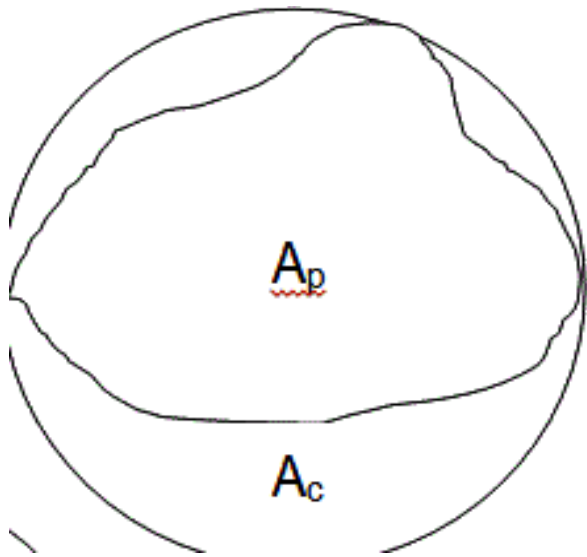
| Shape      | Description   | Examples   |
|------------|---|--|
| Round      | Approaching Spheroid                                | sapota, cherry tomato, pea                           |
| Oblate     | Flattened at the stem end and apex                  | Orange, pumpkin                                      |
| Oblong     | Vertical diameter greater than horizontal diameter  | some apple varieties, capsicum, brinjal, rice, wheat |
| Conic      | Tapered toward the apex                             | ladies finger, carrot, reddish                       |
| Ovate      | Egg shaped & broad at stem end                      | Brinjal, apple and guava.                            |
| Oblique    | Axis connecting stem and apex slanted               | some apple varieties, tomato.                        |
| Obovate    | Inverted ovate-broad at apex                        | Mango, papaya  |
| Elliptical | Approaching ellipsoid                               | rice, wheat, pointed guard etc                       |
| Truncate   | Having both ends squared or flattened               | capsicum   |
| Unequal    | One half larger than the other                      | mango  |
| Ribbed:    | In cross section, sides are more or less angular    | plantain, ladies finger                              |
| Regular    | Horizontal section approaches a circle              | orange, apple, guava etc                             |
| Irregular  | Horizontal section differs materially from a circle | mango, ladies finger, capsicum etc.                  |

# Shape



# ROUNDNESS

- Roundness is a **measure of sharpness of the corners** of the solid. Where, the object area is obtained by projection/tracing.



$$\text{Roundness} = \frac{A_p}{A_c}$$

$A_p$  = largest projected area of object in natural rest position

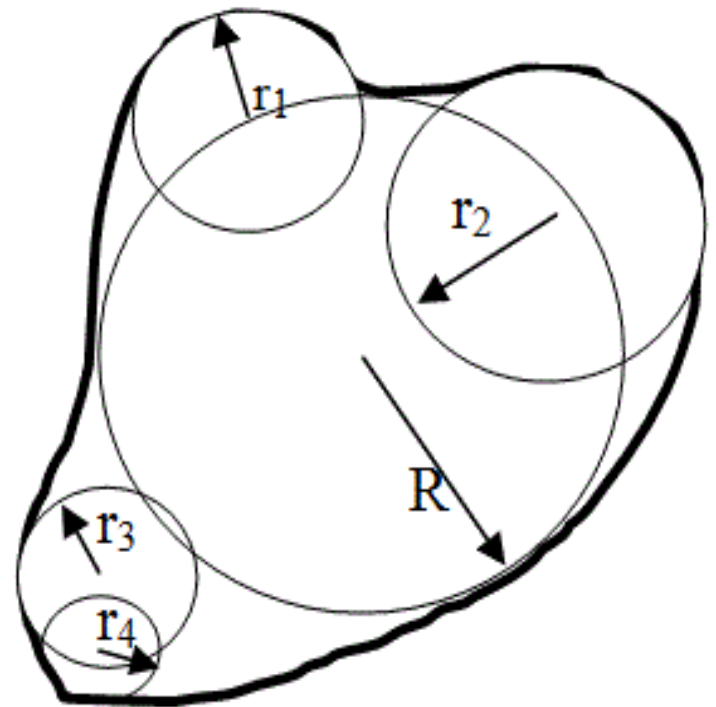
$A_c$  = Area of smallest circumscribing circle

# ROUNDNESS

$$\textit{Roundness} = \frac{\sum r}{NR}$$

Where

- $r$  = radius of curvature of all the corners
- $R$  = Radius of maximum inscribed circle
- **$N$  = total number of corners**



# Numerical

- Q.1. If projected area of a fruit is  $300 \text{ cm}^2$  and the diameter of the smallest circumscribing circle is 10cm. Calculate the Roundness.
- Q.2 If the roundness of a vegetable is 0.95 and the radius of the smallest circle is 3cm, calculate the projected area.
- Q.3 If the radius of sharp corners are 1, 1, and 1.5 cm, whereas the radius of maximum inscribed circle is 5cm, calculate the roundness.

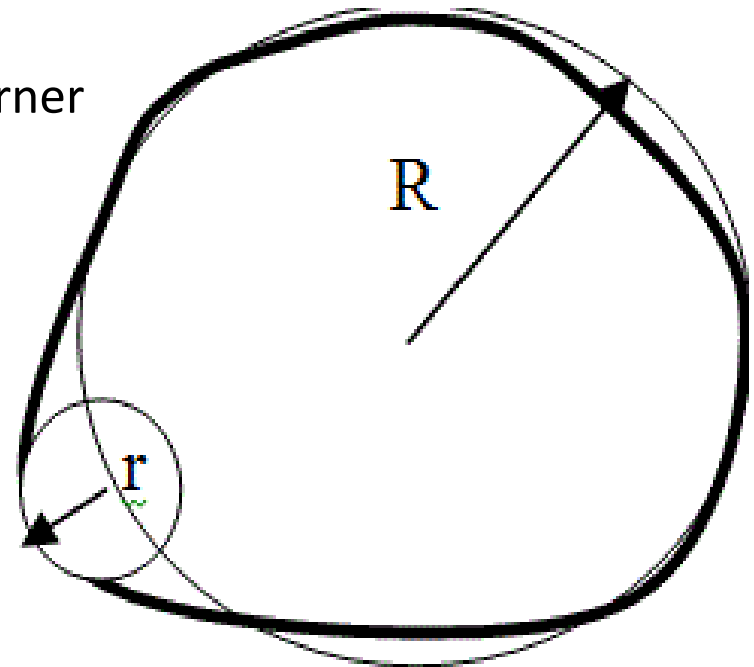
# ROUNDNESS RATIO

$$\text{Roundness ratio} = \frac{r_n}{R_m}$$

**Where**

$R_m$  = mean radius of the object

$r_n$  = radius of curvature of the sharpest corner

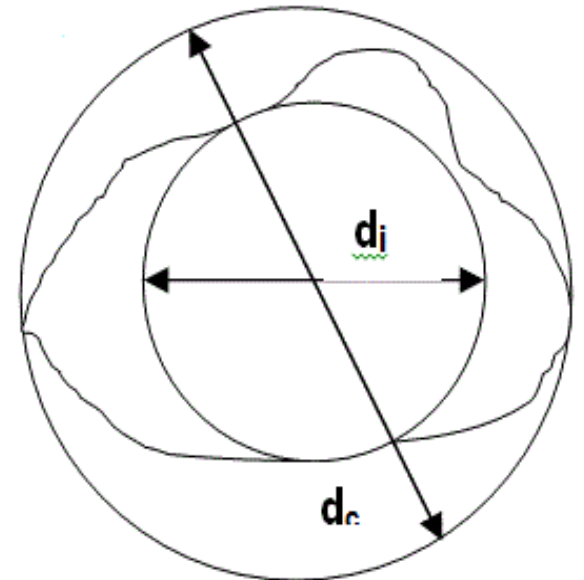


# SPHERICITY

- Sphericity is the degree to which an object resembles a sphere.

$$Sphericity = \frac{d_i}{d_c}$$

- $d_i$  = diameter of largest inscribed circle
- $d_c$  = diameter of smallest circumscribed circle





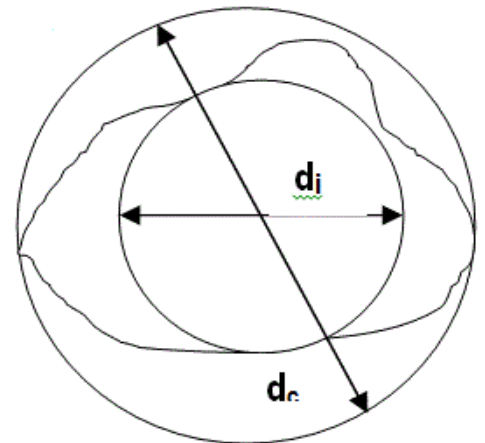
# SPHERICITY

- Sphericity is the degree to which an object resembles a sphere.

$$Sphericity = \frac{d_e}{d_c}$$

Where

- $d_e$  = diameter of the sphere of the same volume as the object
- $d_c$  = diameter of the smallest circumscribed sphere or usually the longest diameter of the object.



# SPHERICITY

$$\begin{aligned} Sphericity &= \left[ \frac{\text{volume of solid}}{\text{volume of circumscribed sphere}} \right]^{\frac{1}{3}} \\ &= \left[ \frac{\frac{\pi}{6} abc}{\frac{\pi}{6} a^3} \right]^{\frac{1}{3}} = \left[ \frac{bc}{a^2} \right]^{\frac{1}{3}} = \frac{[abc]^{\frac{1}{3}}}{a} \end{aligned}$$

Where

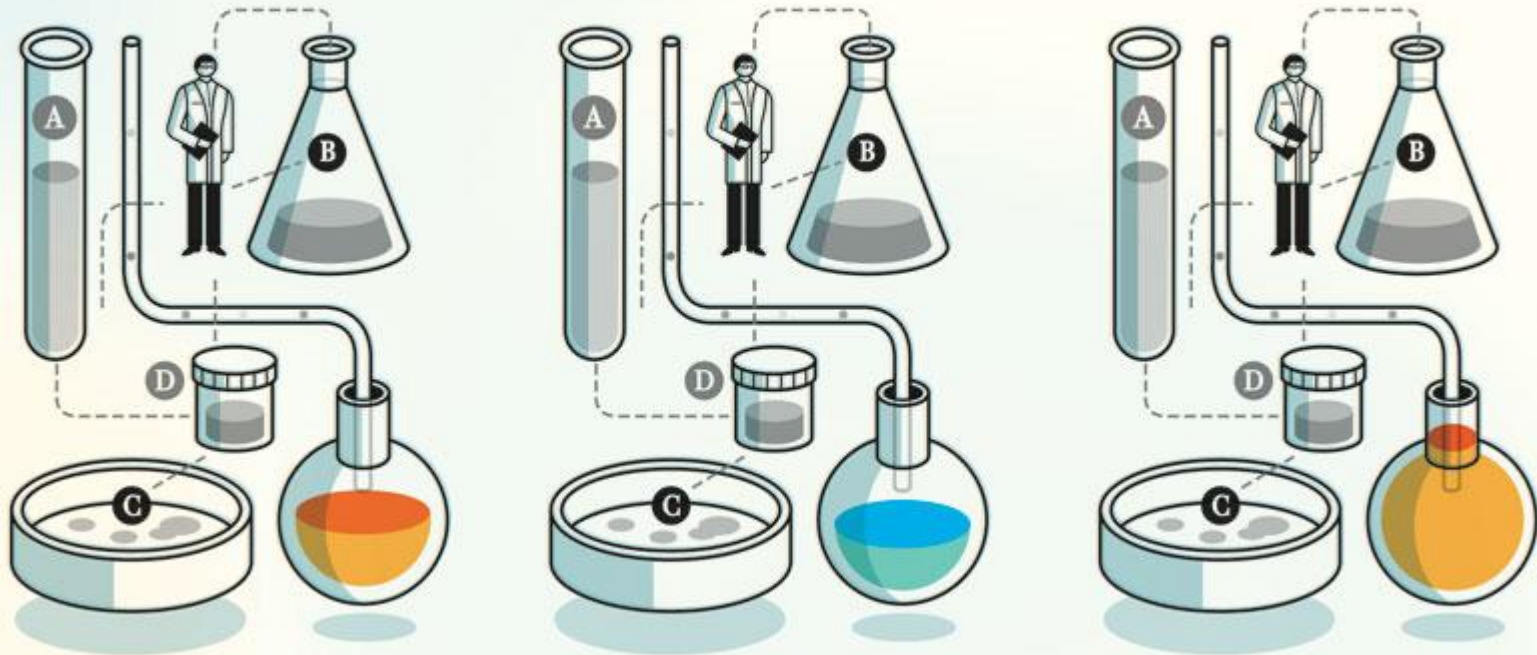
- a = largest intercept
- b = longest intercept normal to a
- c = longest intercept normal to a and b

# Numericals

- Q.1. If largest inscribed and smallest circumscribed radius of a fruit are 4.2 and 5.4cm respectively, calculate the sphericity of the food material.
- Q.2 . If equivalent sphere and smallest circumscribed radius of a fruit are 4.0 and 5.4cm respectively, calculate the sphericity of the food material.
- Q.3 If three intercept of cashew nut are 4, 2.5 and 2.7cm respectively, calculate the sphericity.

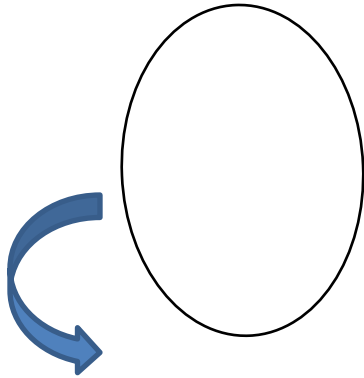
# Replications

- Replication is the act of reproducing or copying something, or is a copy of something.



# Resemblance to geometric bodies

- **Prolate spheroid** which is formed when an ellipse rotates about its major axis.



# Prolate spheroid

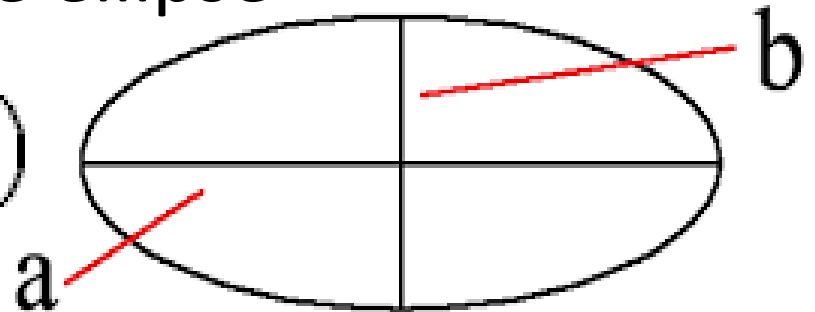
$$V_{\text{prolatespheroid}} = \frac{4}{3}\pi ab^2$$

$$S_{\text{prolatespheroid}} = 2\pi b^2 + 2\pi \frac{ab}{e} \sin^{-1} e$$

Where

- $a$  = major semi axis of the ellipse  $e = \sqrt{1 - \left(\frac{b}{a}\right)^2}$
- $b$  = minor semi axis of the ellipse

where,  $e = \left(1 - \left(\frac{b}{a}\right)^2\right)^{1/2}$

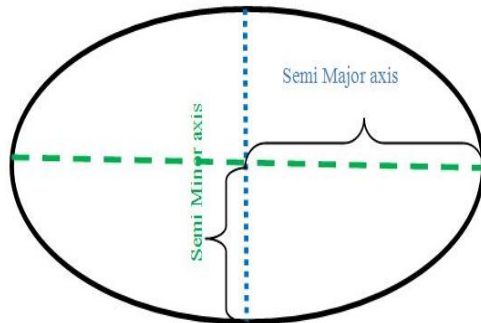


# Numerical

Q.1. If largest and smallest dimension of lemon are 5.2 and 3.4 cm respectively, Calculate the volume and surface area of lemon.

# Oblate spheroid

- **Oblate spheroid** is formed when an ellipse rotates about its minor axis. An oblate spheroid is a rotationally symmetric ellipsoid having a polar axis shorter than the diameter of the equatorial circle whose plane bisects it. e.g. grape fruit, pumpkin





# Oblate spheroid

$$V_{\text{oblatespheroid}} = \frac{4}{3}\pi a^2 b$$

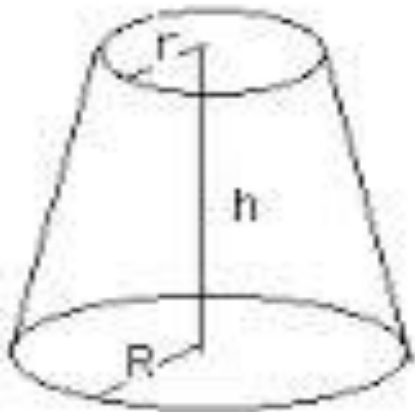
$$S_{\text{oblatespheroid}} = 2\pi a^2 + \pi \frac{b^2}{e} \ln \frac{1+e}{1-e}$$

# Numerical

Q.1. If largest and smallest dimension of pumpkin are 4.3 and 3.4 cm respectively, Calculate the volume and surface area of pumpkin.

# Right circular cone or cylinders

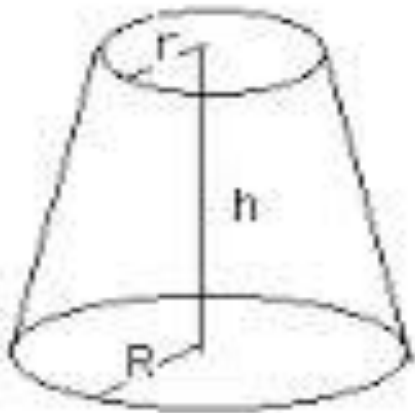
- **Right circular cone or cylinders** is formed when a frustum rotates about its axis e.g. carrot and cucumber.



# Right circular cone or cylinders

$$V_{\text{rightcone}} = \frac{\pi}{3}h[r_1^2 + r_1r_2 + r_2^2]$$

$$S_{\text{rightcone}} = \pi(r_1 + r_2)\sqrt{h^2 + (r_1 - r_2)^2}$$



**Where**

$r_1$  = radius of base

$r_2$  = radius of top (apex)

$h$  = altitude

# Numerical

Q.1. If largest and smallest diameters of carrot are 3.3 and 2.4 cm, whereas the length of carrot is 12 cm, Calculate the volume and surface area of carrot.

# Correction factor

- **Actual Volume**

= Correction factor<sub>1</sub> X Estimated volume



- **Actual surface area**

= Correction factor<sub>2</sub> X Estimated volume



# Grading of rice: Interrelations

- Slenderness ratio  $\Rightarrow$  Length : width
- Aspect ratio  $\Rightarrow$  Width: length

# Grading of fruit: Interrelations

- Ellipsoid ratio  $\Rightarrow$  Major diameter: minor diameter
- Aspect ratio  $\Rightarrow$  length: major diameter